

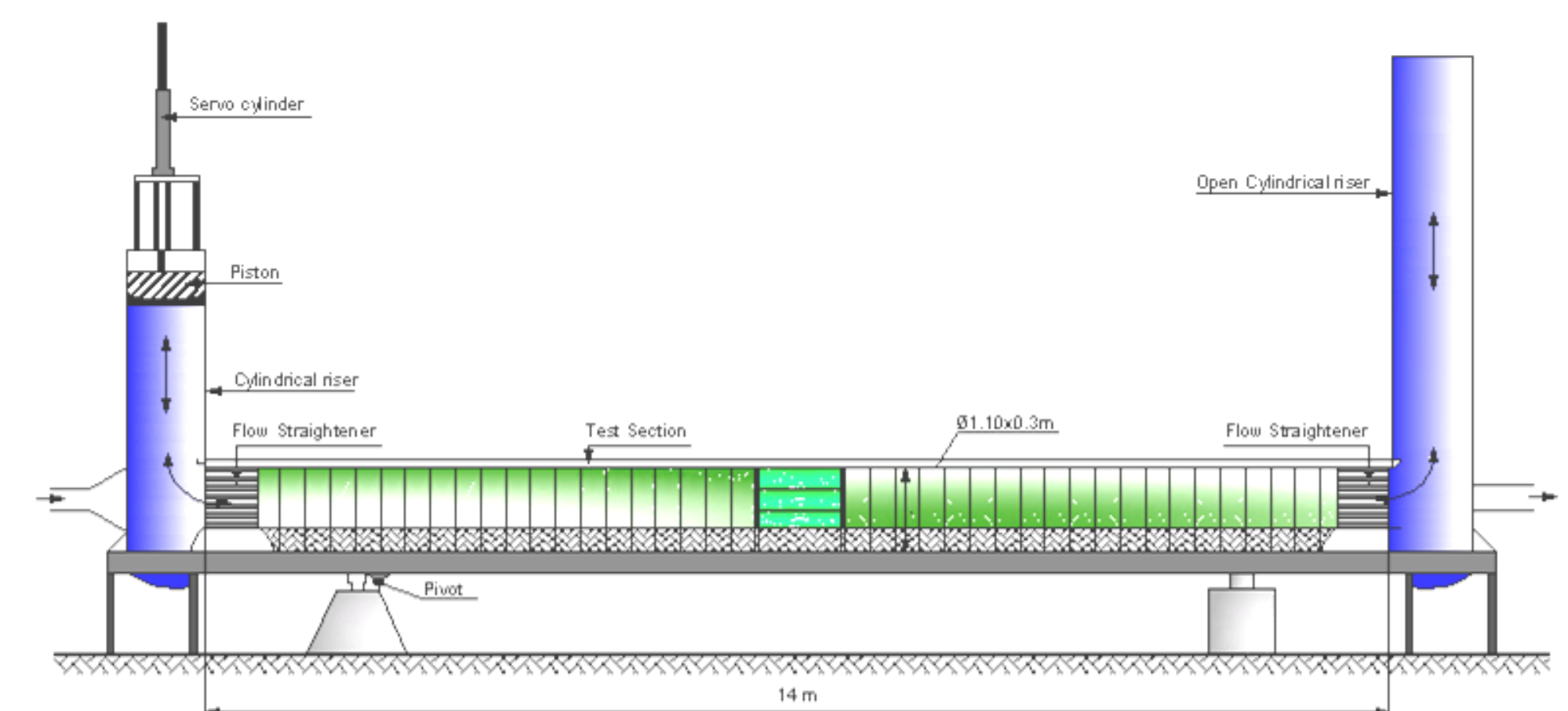
# Velocity defect law in the wave bottom boundary layer

## Objective

This work presents a simple method based on the defect law (Nielsen, 1992) to reproduce the velocity vertical profile within the wave bottom boundary layer.

## TRANSKEW experiment

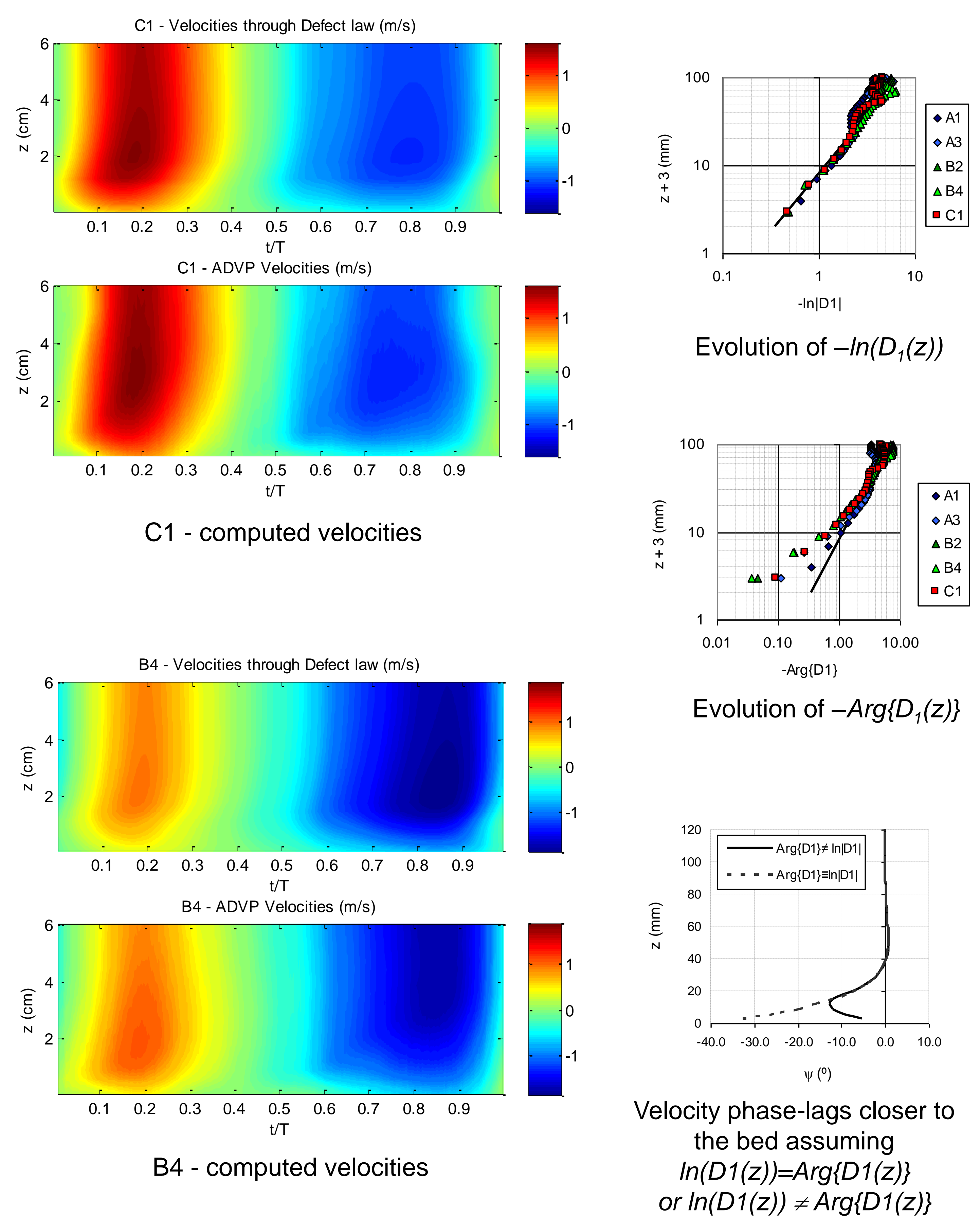
- New series of experiments to evaluate the net transport rates in **sheet flow regime**, (well-sorted sand bed,  $d_{50} \approx 0.20$  mm), under accelerated skewed waves, (Silva *et al.*, 2010).
- Different hydraulic conditions
  - **Series A:** regular oscillatory flows with different degrees of acceleration skewness,  $\beta$ ;
  - **Series B:** acceleration-skewed oscillatory flows with a collinear net current, opposing the wave direction;
  - **Series C:** velocity- and acceleration- skewed oscillatory flows.
- An Acoustic Doppler Velocity Profiler (ADVP) measured simultaneously both horizontal and vertical velocities every 3mm over a 14cm layer immediately above the bed.



Condition	$\beta^a$	$R^b$	$T^c$ [s]	$U_0^d$ [m/s]
A1	0.65	0.5	7	0
A2	0.65	0.5	10	0
A3	0.75	0.5	7	0
A4	0.75	0.5	10	0
B1	0.65	0.5	7	-0.2
B2	0.65	0.5	7	-0.4
B3	0.75	0.5	7	-0.2
B4	0.75	0.5	7	-0.4
C1	0.65	0.6	7	0
C2	0.65	0.6	10	0
C3	0.50	0.6	7	0

<sup>a</sup>  $\beta$  is acceleration skewness,  $a_{\max}/(a_{\max} - a_{\min})$ , where  $a$  is acceleration  
<sup>b</sup>  $R$  is velocity skewness,  $u_{\max}/(u_{\max} - u_{\min})$ , where  $u$  is velocity  
<sup>c</sup>  $T$  is wave period  
<sup>d</sup>  $U_0$  is net current

## Results



## Analysis Procedure

### DEFECT LAW

- the velocities  $u(z,t)$  inside the wave bottom boundary layer can be written in terms of the free stream velocity,  $u_{\infty}(t)$ , and a dimensionless velocity defect function  $D_1(z)$ :

$$u(z,t) = [1 - D_1(z)] u_{\infty}(t) \quad (1)$$

- Nielsen (1992) suggested that, for turbulent flows,  $D_1(z)$  requires the knowledge of a vertical scale,  $z_1$ , and a power  $p$  that fits the data:

$$-\ln|D_1(z)| = \left(\frac{z}{z_1}\right)^p \quad (2)$$



ADVPprofiler

- An analysis of the primary harmonic of the velocity records from ADVP pointed  $z_1 \approx 8\text{mm}$  and  $p \approx 0.75$  for all the experiments.

- Abreu *et al.* (2010) showed that an arbitrary nonlinear free stream velocity,  $u_{\infty}(t)$ , can be represented according to 4 parameters ( $U_w, T, r, \phi$ ):

$$u_{\infty}(t) = U_w \sqrt{1-r^2} \frac{\left[ \sin(\omega t) + \frac{r \sin \phi}{1 + \sqrt{1-r^2}} \right]}{[1 - r \cos(\omega t + \phi)]} \quad (3)$$

- Eq. (2) was combined with Eq. (3) to reproduce  $u(z,t)$  inside the wave bottom boundary layer.

## Main Conclusions

- The model results agree fairly well with the ADVP measurements and show that the defect law reproduces typical features of the oscillatory boundary layer: the velocity magnitude first increases with distance from the bed, with an overshoot at approximately 3 cm above the bed.
- There is a phase shift in the velocity that is maximum at about 1cm above the bed.
- Processing of the bed shear stress as well as velocities estimates within the sheet flow layer is under progress. (e.g. Ruessink *et al.*, submitted)

## REFERENCES

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